

6'.2 Homework

1. Let f be a function that has derivatives of all orders for all real numbers.

Assume that $f(0) = 5$, $f'(0) = -3$, $f''(0) = 8$, and $f'''(0) = 24$.

Write the third order Taylor polynomial for f at $x = 0$ and use it to approximate $f(0.4)$.

2. Find the interval of convergence for $\sum_{n=0}^{\infty} \frac{(4x-3)^{3n}}{8^n}$.

3. Determine if $\sum_{n=1}^{\infty} \frac{1}{3^n + 2}$ converges. Show your work.

4. Determine if the series converges absolutely, conditionally, or diverges.

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{n^3 - \ln n}.$$