

**LC Math 1 Adv - Re-Writing Standard Form Equations in Vertex Form (LT 10)**

Determine what number "c" must be added to each expression to complete the square, then re-write the trinomial as the square of a binomial.

1.  $x^2 + 6x + c$

$$\begin{aligned} x^2 + 6x + 9 \\ \underline{\underline{(x+3)^2}} \end{aligned}$$

2.  $x^2 - 10x + c$

$$\begin{aligned} x^2 - 10x + 25 \\ \underline{\underline{(x-5)^2}} \end{aligned}$$

3.  $x^2 + 14x + c$

$$\begin{aligned} x^2 + 14x + 49 \\ \underline{\underline{(x+7)^2}} \end{aligned}$$

4.  $x^2 - 8x + c$

$$\begin{aligned} x^2 - 8x + 16 \\ \underline{\underline{(x-4)^2}} \end{aligned}$$

Re-write each standard form equation in vertex form.

5.  $y = x^2 + 16x + 71$

$$y = (x^2 + 16x + 64) + 71 - 64$$

$$\boxed{y = (x+8)^2 + 7}$$

6.  $y = x^2 - 2x - 5$

$$y = (x^2 - 2x + 1) - 5 - 1$$

$$\boxed{y = (x-1)^2 - 6}$$

7.  $y = -2x^2 - 20x - 53$

$$y = -2(x^2 + 10x + 25) - 53 + 50$$

$$\boxed{y = -2(x+5)^2 - 3}$$

8.  $y = 3x^2 - 12x + 8$

$$y = 3(x^2 - 4x + 4) + 8 - 12$$

$$\boxed{y = 3(x-2)^2 - 4}$$

Graph each function below on the coordinate planes provided. Include the vertex, axis of symmetry, and four additional points.

9.  $f(x) = -\left(x - \frac{5}{2}\right)^2 + 2$

Vertex:  $\left(\frac{5}{2}, 2\right)$

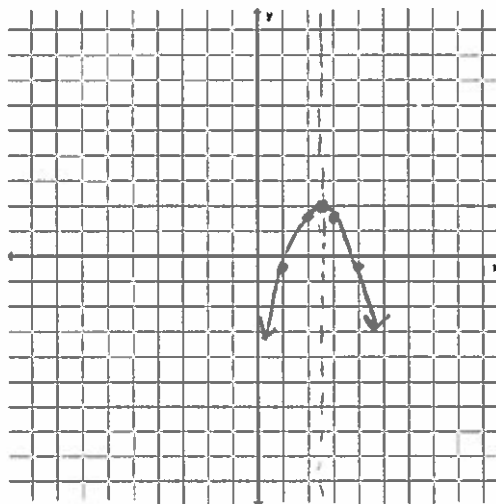
Axis of Symmetry:  $x = \frac{5}{2}$

Additional Points:  $(3, \frac{7}{4})$

and \_\_\_\_\_

$$f(3) = -\left(3 - \frac{5}{2}\right)^2 + 2 = -\frac{1}{4} + 2 = \frac{7}{4}$$

$$f(4) = -\left(4 - \frac{5}{2}\right)^2 + 2 = -\frac{9}{4} + 2 = -\frac{1}{4}$$



10.  $f(x) = x^2 - 8x + 14$

$$f(x) = (x^2 - 8x + 16) + 14 - 16$$

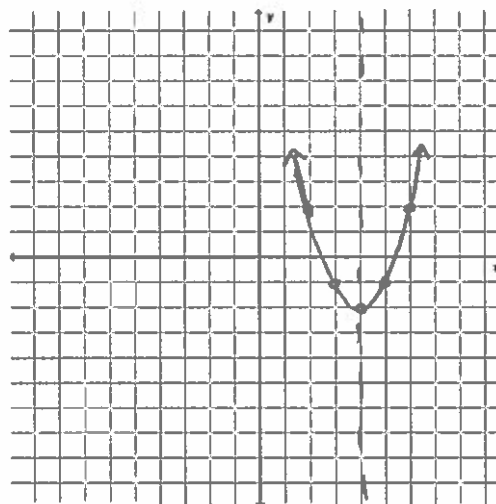
$$f(x) = (x - 4)^2 - 2$$

Vertex:  $(4, -2)$

Axis of Symmetry:  $x = 4$

Additional Points:  $(5, -1)$

and  $(6, 2)$



11.  $f(x) = -2x^2 + 6x + 3$

$$(-2x^2 + 6x) + 3$$

$$-2\left(x^2 - 3x + \frac{9}{4}\right) + 3 + \frac{9}{2}$$

$$-2\left(x - \frac{3}{2}\right)^2 + \frac{15}{2}$$

Vertex:  $\left(\frac{3}{2}, \frac{15}{2}\right)$

Axis of Symmetry:  $x = \frac{3}{2}$

Additional Points:  $(2, 7)$

and  $(3, 3)$

$$f(2) = -2\left(\frac{2}{2}\right)^2 + \frac{15}{2} = 7$$

$$f(3) = -2\left(\frac{3}{2}\right)^2 + \frac{15}{2} = 3$$

$$-\frac{9}{2} + \frac{15}{2}$$

